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Formula flashcards for Pearson Edexcel iGCSE Mathematics (4MA1) and Further Pure Mathematics (4PM1)

by Kirsty

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Foundation Tier (4MA1)

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Formula not given in exam

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Pythagoras Theorem

 $a^2 + b^2 = c^2$

- only applies to right angle triangles
- used to find the length of sides



Area of a rectangle

 $l \times w$



Area of triangle $\frac{1}{2}b \times h$



- sometimes, the diagonal is given so you can use pythagoras theorem to find h

Area of parallelogram

 $b \times h$

- use pythagoras theorem to find h



Volume of cuboid

$l \times w \times h$



Circumference of a circle



- may also be written as 'perimeter' in exam Qs



Area of a circle





- always pay attention to the units given and the units they want in your answer

Trigonometric ratios (right-angled triangles)

sine $x = \frac{0}{h}$ o = opposite a = adjacent h = hypotenuse $\cos x = \frac{a}{h}$ remember: sOH cAH tOA $\tan x = \frac{0}{a}$



nth term (arithmetic series)

$$\mathbf{u}_{\mathbf{n}} = \mathbf{a} + (\mathbf{n} - 1)\mathbf{d}$$

a = first term

d = common difference

n = number of terms

Formula given in exam

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Area of trapezium

 $\frac{1}{2}(a+b)h$

- use pythagoras theorem to find h



Volume of prism

- cross section area \times length
 - applicable to any prism



Curved surface area of cylinder $2\pi rh$

- curved area + area of 2 circle (top + base) = total surface area







Higher Tier (4MA1)

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nth term (arithmetic series)

$$\mathbf{u}_{\mathbf{n}} = \mathbf{a} + (\mathbf{n} - 1)\mathbf{d}$$

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n = number of terms

Volume of pyramid

$\frac{1}{3} \times base area \times h$

- applicable to any pyramid



Sector arc length $2\pi r \times \frac{\theta}{360}$

- perimeter = arc length + 2r

Area of a sector

$$\pi r^2 \times \frac{\theta}{360}$$



Formula given in exam

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Area of trapezium

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 - applicable to any prism



Quadratic Formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

- for $ax^2 + bx + c = 0$
- will give 2 values of x

Sine rule





- used to find a side or angle by using its opposing angle or side respectively

example:



Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$



- used to find a side by using 2 given sides and its opposing angle

example:





Area of triangle (non-right angle)

- $\frac{1}{2}$ ab sinC
- used to find the area by using 2 sides and 1 angle (not opposing any of the given sides)



Curved surface area of cone πrl

- curved surface area + circle (base) area = total surface area

h r

Volume of cone



Sum to n terms (arithmetic series)

$$\mathbf{S}_{\mathbf{n}} = \frac{\mathbf{n}}{2} [2\mathbf{a} + (\mathbf{n} - 1)\mathbf{d}]$$

a = first term

d = common difference

n = number of terms

Surface area of sphere

 $4\pi r^2$

Volume of sphere





Further Pure Mathematics (4PM1)

Formula not given in exam

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Trigonometric ratios (right-angled triangles)

sine $x = \frac{0}{h}$ o = opposite a = adjacent h = hypotenuse $\cos x = \frac{a}{h}$ remember: sOH cAH tOA $\tan x = \frac{0}{a}$



nth term (arithmetic series)

$$\mathbf{u}_{\mathbf{n}} = \mathbf{a} + (\mathbf{n} - 1)\mathbf{d}$$

a = first term

d = common difference

n = number of terms

nth term (geometric series)

 $u_n = ar^{n-1}$

a = first term

r = common ratio

n = number of terms

Volume of pyramid

$\frac{1}{3} \times base area \times h$

- applicable to any pyramid



Sector arc length

degrees:

radians:

 $\frac{\theta}{360}$ $2\pi r \times$

 $l = r\theta$



 $180^{\circ} = \pi rad$

Area of a sector

degrees:



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radians:

Logarithms

$$\begin{split} \log_{a}(xy) &= \log_{a}(x) + \log_{a}(y) \\ \log_{a}\left(\frac{x}{y}\right) &= \log_{a}(x) - \log_{a}(y) \\ \log_{a}\left(x^{k}\right) &= k\log_{a}(x) \\ n\log_{a}(b) &= \frac{n}{\log_{b}(a)} \end{split}$$

Roots (quadratics)

$$\alpha + \beta = -\frac{b}{a}$$
$$\alpha\beta = \frac{c}{a}$$

- $\mathbf{x}^2 (\alpha + \beta) + \alpha\beta = 0$
- for $ax^2 + bx + c$

additional: $\alpha^2 + \beta^2 = (\alpha^2 + \beta^2) - 2\alpha\beta$ $\alpha^2 - \beta^2 = (\alpha - \beta)(\alpha + \beta)$ $\alpha^3 + \beta^3 = (\alpha + \beta)(\alpha^2 + \alpha\beta + \beta^2)$ $\alpha^4 - \beta^4 = \left(\alpha^2 + \beta^2\right)^2 - 2(\alpha\beta)^2$ $\alpha - \beta = \sqrt{(\alpha + \beta)^2 - 4\alpha\beta}$

Coordinate geometry

Gradient

Distance between 2 points

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$d^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2$$

Coordinates of the point dividing the line in a given ratio

m:n

$$(\frac{nx_1 + mx_2}{m+n}, \frac{ny_1 + my_2}{m+n})$$

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Differentiation

 $x^n = nx^{n-1}$

 $\sin ax = a\cos ax$

 $\cos ax = -a\sin ax$

 $e^{ax} = ae^{ax}$

Chain rule

$$\int f(g(x)) = f'(g(x))g'(x)$$

Product rule

$$\frac{\mathrm{d}}{\mathrm{dx}}(\frac{\mathrm{f}(\mathrm{x})}{\mathrm{g}(\mathrm{x})}) = \mathrm{f}'(\mathrm{x})\mathrm{g}(\mathrm{x}) + \mathrm{f}(\mathrm{x})\mathrm{g}'(\mathrm{x})$$

Integration

$$\int x^{n} = \frac{1}{n+1} x^{n+1} + c$$
$$\int \sin ax = -\frac{1}{a} \cos ax + c$$
$$\int \cos ax = \frac{1}{a} \sin ax + c$$
$$\int e^{ax} = \frac{1}{a} e^{ax} + c$$

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Area between two lines



- top line - bottom line



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Volume of revolution

 $\int_a^b \pi \ y^2 \, dx$

- if a curve was rotated 360° to form a 3D shape



Trigonometry Identities

- $\sin^2\!\theta + \cos^2\!\theta = 1$
- the rest are given in the formula sheet

Formula given in exam

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Sum to n terms (arithmetic series)

$$\mathbf{S}_{\mathbf{n}} = \frac{\mathbf{n}}{2} [2\mathbf{a} + (\mathbf{n} - 1)\mathbf{d}]$$

a = first term

d = common difference

n = number of terms

Curved surface area of cone πrl

- curved surface area + circle (base) area = total surface area



Surface area of sphere

 $4\pi r^2$

Volume of sphere





Sum to n terms (geometric series) $S_n = \frac{a(1 - r^n)}{1 - r}$

a = first term

r = common ratio

n = number of terms

Sum to infinity

$$S_{\infty} = \frac{a}{1-r}$$

a = first term

r = common ratio

- when $-1 \le r \ge 1$

Binomial series

$$(1+x)^{n} = 1 + nx + \frac{n(n-1)}{2!}x^{2} + \frac{n(n-1)\dots(n-r+1)}{r!} + \dots$$

- when -1 < x < 1

Quotient rule (differentiation)

$$\frac{\mathrm{d}}{\mathrm{dx}} \left(\frac{\mathrm{f}(\mathrm{x})}{\mathrm{g}(\mathrm{x})} \right) = \frac{\mathrm{f}'(\mathrm{x})\mathrm{g}(\mathrm{x}) - \mathrm{f}(\mathrm{x})\mathrm{g}'(\mathrm{x})}{\left[\mathrm{g}(\mathrm{x})\right]^2}$$

Trigonometry identities

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A + B) = \sin A \cos B + \cos A \sin B \qquad \sin(A - B) = \sin A \cos B - \cos A \sin B$$
$$\cos(A + B) = \cos A \cos B - \sin A \sin B \qquad \cos(A - B) = \cos A \cos B + \sin A \sin B$$
$$\tan(A + B) = \frac{\tan A + \tan B}{1 - \tan A \tan B} \qquad \tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_{a}(x) = \frac{\log_{b}(x)}{\log_{b}(a)}$$

- b can be any number as long as b > 1

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Acknowledgements and Information:

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